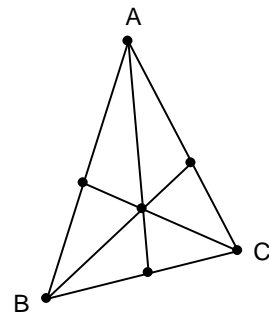


2009 Triangle Topic Test (Theta)

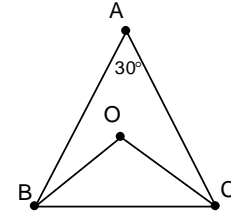
- Find the area of a triangle whose sides are 10, 12, and 14.
 A. 60 B. $96\sqrt{33}$ C. 30 D. $24\sqrt{6}$ E. NOTA
- The legs of a right triangle are 5 and 10, while the hypotenuse of a similar triangle is 15. What is the area of the larger triangle?
 A. 90 B. $15+9\sqrt{5}$ C. 45 D. 25 E. NOTA
- The area of $\triangle ABC$ is 112 and its altitude to \overline{AB} is 4. Find the length of the median to \overline{AB} if its projection on \overline{AB} is 3.
 A. $112\sqrt{3}$ B. 5 C. $5\sqrt{7}$ D. 100 E. NOTA
- $\triangle ABC$ has an area of 240 square inches. $AB = 20$ inches. Find the area of the trapezoid formed when a line is drawn parallel to \overline{AB} and 8 inches from C .
 A. $\frac{640}{3}$ B. $\frac{80}{3}$ C. 160 D. $20\sqrt{3}$ E. NOTA
- The area of a circle circumscribed about an equilateral triangle is 196π square inches. Find the altitude of the triangle.
 A. 14 B. 21 C. 36 D. 196 E. NOTA
- In $\triangle ABC$, $AB = 24$ inches. \overline{PQ} is drawn parallel to \overline{AB} so that P and Q are on \overline{AC} and \overline{BC} respectively and the area of $\triangle CPQ$ is equal to one third the area of $\triangle ABC$. Find PQ .
 A. 8 B. 16 C. $8\sqrt{3}$ D. $24\sqrt{3}$ E. NOTA
- In a triangle whose sides are 6, 7, 8, determine the longer of the two segments into which the bisector of the largest angle divides the opposite side.
 A. $\frac{16}{3}$ B. $\frac{48}{13}$ C. $\frac{8}{3}$ D. $\frac{56}{13}$ E. NOTA
- $\triangle ABC$ has sides of length 4, 5, and 6. If $\triangle A'B'C'$ is similar to $\triangle ABC$ but has three times the area, find the perimeter of $\triangle A'B'C'$.
 A. 21 B. $9\sqrt{3}$ C. $15\sqrt{3}$ D. 45 E. NOTA
- In $\triangle ABC$, the measures of $\angle BAC$ and $\angle ABC$ are 44 and 58 degrees respectively. Find the measure of the largest of the (non-overlapping) angles formed by the intersection bisectors of the $\angle A$, $\angle B$, and $\angle C$.



- A. 72° B. 36° C. 58° D. 68° E. NOTA

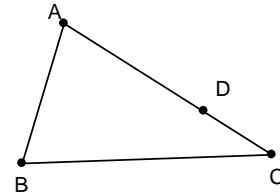
2009 Triangle Topic Test (Theta)

10. In isosceles $\triangle ABC$, $AB = AC$ and measure of angle A is 30° degrees. From a point O within the triangle \overline{OB} and \overline{OC} are drawn such $m\angle CBO = m\angle ACO$. $m\angle BOC = ?$



- A. 90° B. 100° C. 105° D. 110° E. NOTA

11. In $\triangle ABC$, $AC > AB$. Point D is chosen on \overline{AC} so that $AD = AB$. If $m\angle CBA - m\angle C = 20^\circ$, then $m\angle CBD = ?$

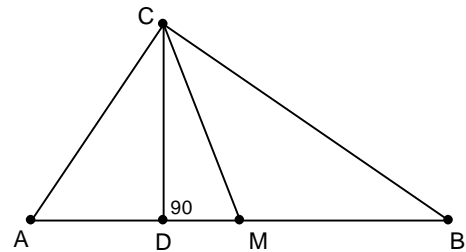


- A. 10° B. 15° C. 20° D. 25° E. NOTA

12. If the legs of a right triangle are represented by a and b and the hypotenuse by c , and if c and a are consecutive integers, then b^2 is

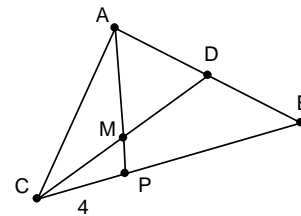
- A. $c - a$ B. $c + a$ C. ca D. c/a E. NOTA

13. In right $\triangle ABC$, with median \overline{CM} and altitude \overline{CD} , $m\angle MCD = \frac{1}{2}m\angle A$, $m\angle A > m\angle B$. $m\angle MCD = ?$



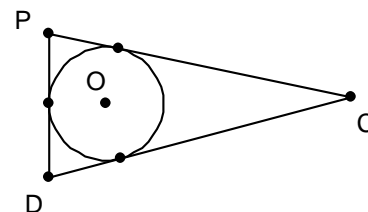
- A. 18° B. 36° C. 30° D. 34° E. NOTA

14. In $\triangle ABC$, the median from C meets \overline{AB} in D . \overline{AM} is drawn through M , the midpoint of \overline{CD} , and intersects \overline{CB} at P . If $CP = 4$, then CB is



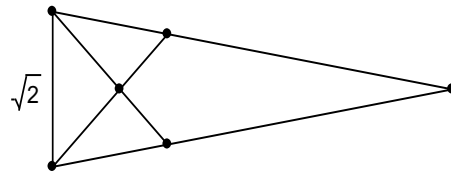
- A. 6 B. 8 C. 10 D. 12 E. NOTA

15. $\triangle PCD$ is formed by three tangents to circle O . If $m\angle P = 30^\circ$, then $m\angle COD = ?$



- A. 105° B. 75° C. 150° D. 60° E. NOTA

16. The base of an isosceles triangle is $\sqrt{2}$; medians to the legs intersect at right angles. The area of the given triangle is



- A. 1.5 B. 5 C. 2.5 D. 3 E. NOTA

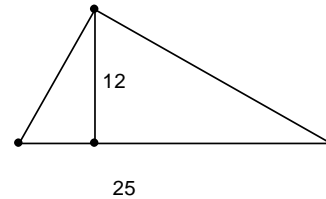
17. The medians of a triangle are 30 inches, 30 inches and 48 inches. The area of the triangle is

- A. 524 B. 554 C. 576 D. 596 E. NOTA

18. If the hypotenuse of an isosceles right triangle is 10 find the length of the altitude to the hypotenuse.

- A. $5\sqrt{2}$ B. $5\sqrt{3}$ C. $2\sqrt{2}$ D. $3\sqrt{2}$ E. NOTA

19. The hypotenuse of a right triangle is 25. If the altitude from the right angle to the hypotenuse is 12, what is the length of the longest segment it forms on the hypotenuse?



- A. 8 B. 15 C. 16 D. 20 E. NOTA

20. The triangle with vertices $(-2, 1)$, $(2, 4)$, and $(3, 1)$ is

- A. scalene B. equilateral C. isosceles D. right E. NOTA

21. In $\triangle ABC$, $AB = 7$, $BC = 8$, and $AC = 5$. Find the projection of \overline{BC} upon \overline{CA} .

- A. 2 B. 4 C. 6 D. 8 E. NOTA

22. Two sides of a triangle are 6 ft and 10 ft with an included angle of 120° . Find its area.

- A. $\frac{39\sqrt{3}}{2}$ B. $\frac{55\sqrt{3}}{2}$ C. $45\sqrt{3}$ D. $15\sqrt{3}$ E. NOTA

23. What is the radius of a circle inscribed in a triangle whose sides measure 50, 30, and 40?

- A. 25 B. 20 C. 15 D. 10 E. NOTA

24. Right $\triangle ABC$ has legs of 3" and 4". The locus of points equidistant from the sides of the triangle is a point whose distance from the sides is

- A. 1" B. 2" C. 2.5" D. 3" E. NOTA

25. The angle bisectors of a triangle are concurrent in a point known as the

- A. incenter B. circumcenter C. orthocenter D. point of Euler E. NOTA

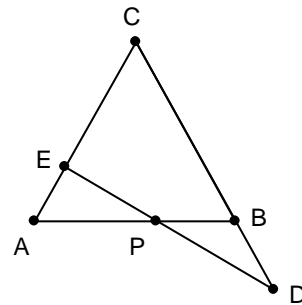
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26. $\triangle ABC$ has an area of 40 sq. in. Side $AB = 10''$ and is fixed in position. The locus of C is a
 A. \perp bisector B. \angle bisector C. line \parallel to \overline{AB} D. set of lines \parallel to \overline{AB} E. NOTA

27. The radius of a circle inscribed in equilateral $\triangle ABC$ whose side is 6 inches is equal to
 A. $\frac{2}{3}\sqrt{3}$ B. $\frac{1}{3}\sqrt{3}$ C. $\sqrt{3}$ D. $\frac{1}{2}\sqrt{3}$ E. NOTA

28. Fixed points A and B are 10" apart. Point P moves so that $\overline{PA} \perp \overline{PB}$. The locus of P is a
 A. \odot radius 10" B. \odot radius 5" C. \angle bisector D. \perp bisector E. NOTA

29. In the adjacent sketch, $m\angle CDE = 20^\circ$. Find $m\angle A$ if $CB = CA$; P is any point on \overline{AB} ; \overline{CB} is extended to D so that $BD = BP$ and \overline{DP} extended meets \overline{AC} in E .



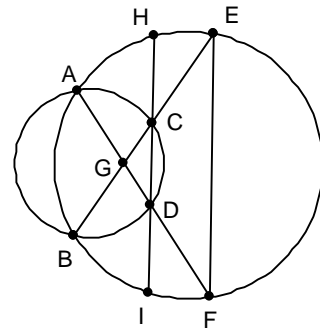
- A. 100° B. 80° C. 60° D. 40° E. NOTA
30. In $\triangle ABC$ $b = 10$, $c = 6$, and $m\angle A = 150^\circ$, find a .
 A. $2\sqrt{21}$ B. $\frac{61}{3}$ C. $\frac{97}{10}$ D. 16 E. NOTA

Tiebreaker #1

Quadrilateral $ABCD$ has its vertices on a circle. $m\angle B = 3x + 25$; $m\angle D = 3x + 35$; $m\angle D = 7x + 15$; Find the measure of the largest angle in triangle $\triangle BCD$.

Tiebreaker#2

Given that $\overline{HI} \parallel \overline{EF}$; $m \text{ arc } EF = 160^\circ$; $\overline{GC} \cong \overline{GD}$, $m \text{ arc } HI = 150^\circ$ and $m\angle ECD = 142^\circ$, find $m\angle AGE$



Tiebreaker#3

\overline{AF} , \overline{BD} , and \overline{CE} are concurrent line segments in the given figure. Find the value of $\frac{x}{y}(z)$.

