

1.	6	8.	-33
2.	$-\frac{328}{25}$ or equivalent	9.	0
3.	$-\frac{5}{48}$	10.	-1973
4.	$5700\pi$	11.	$-522 + 10\sqrt{3}$
5.	$\sin x$	12.	$\frac{18}{5}$ or equivalent
6.	-30	13.	916
7.	$\frac{5}{4}y$	14.	$-180\pi\sqrt{17}$

$$1. x^2 + 4x + 4 = A(x^2 + 2) + (Bx + C)(x - 1) \quad A = 3 \rightarrow B = -2 \rightarrow C = 2$$

$$\frac{x^2(x-2) + (x-2)}{(x-6)(x+1)} = \frac{(x^2+1)(x-2)}{(x-6)(x+1)} \rightarrow 2VA$$

$$\frac{5x^2(2x-3) + 1(2x-3)}{9x^2(2x-3) + 4(2x-3)} = \frac{(5x^2+1)(2x-3)}{(9x^2+4)(2x-3)} \rightarrow 0VA$$

$$\frac{(15x-2)(3x+4)}{4(15x^2-17x+2)} = \frac{(15x-2)(3x+4)}{(15x-2)(x-1)} \rightarrow 1VA$$

$$3 - 2 + 2 + 2 + 0 + 1 = 6$$

$$2. \sin x \cos y + \sin y \cos x = \frac{-3}{5} \cdot \frac{24}{25} + \frac{7}{25} \cdot \frac{4}{5} = \frac{-44}{125}$$

$$\frac{\tan x - \tan y}{1 + \tan x \tan y} = \frac{\frac{5}{12} - \frac{-5}{12}}{1 - \frac{5}{12} \cdot \frac{-5}{12}} = \frac{120}{119}$$

$$1 - 4\theta + 7 + 10\theta = 90 \rightarrow 6\theta = 82 \rightarrow \theta = \frac{41}{3}$$

$$\frac{169ABC}{44} = \frac{-328}{25}$$

$$3. A = \text{Ratio of coefficients of highest power terms} \rightarrow \frac{\sqrt{4x^2}}{x} = \frac{2x}{x} = 2$$

$$B = 1^2 + 4 = 5$$

$$C = \frac{\left(\frac{1}{x+4} - \frac{1}{4}\right)}{x} \cdot \frac{4(x+4)}{4(x+4)} = \frac{4 - (x+4)}{4x(x+4)} = \frac{-1}{4(x+4)} = \frac{-1}{16}$$

$$D = \frac{3 - \sqrt{x+6}}{3-x} \cdot \frac{3 + \sqrt{x+6}}{3 + \sqrt{x+6}} = \frac{9 - (x+6)}{(3-x)(3 + \sqrt{x+6})} = \frac{1}{3 + \sqrt{x+6}} = \frac{1}{6}$$

$$ABCD = \frac{-5}{48}$$

$$4. A = \frac{20 \text{ rev}}{\text{sec}} \cdot \frac{60 \text{ sec}}{\text{min}} \cdot \frac{2\pi \text{ rad}}{1 \text{ rev}} = 2400\pi$$

$$B = \frac{1 \text{ rev}}{42 \text{ sec}} \cdot \frac{60 \text{ sec}}{1 \text{ min}} \cdot \frac{330\pi}{1 \text{ rev}} = 3300\pi$$

$$A + B = 5700\pi$$

$$5. \frac{\sin(2x+x) - \sin(2x-x)}{\cos(2x-x) + \cos(2x+x)} = \frac{\sin 2x \cos x + \cos 2x \sin x - \sin 2x \cos x + \cos 2x \sin x}{\cos 2x \cos x + \sin 2x \sin x + \cos 2x \cos x - \sin 2x \sin x}$$

$$\frac{2 \cos 2x \sin x}{2 \cos 2x \cos x} = \frac{\sin x}{\cos x} = \tan x$$

$$\frac{\tan x}{\csc x + \cot x} \cdot \frac{\csc x - \cot x}{\csc x - \cot x} = \frac{1}{\cos x} - 1 = \sec x$$

$$\frac{A}{B} = \frac{\tan x}{\sec x} = \sin x$$

$$6. \cos A = \frac{Y^2 + Z^2 - X^2}{2YZ} = \frac{X^2}{2X^2} = \frac{1}{2} \rightarrow A = 60$$

$$x^2 - 6x + 9 + y^2 - 8y + 16 = -21 + 9 + 16 \quad (x-3)^2 + (y-4)^2 = 4$$

Use distance formula to find distance from point to center. This distance is  $2\sqrt{2}$ . The radius is 2. This forms a 45-45-90 right triangle so the answer is 90.

$$60 - 90 = -30$$

$$7. A = (\log_2 - 3)(\log_2 x + 2) = 0 \rightarrow x = 8 \text{ and } \frac{1}{4} \text{ so product is } 2.$$

$$B = 2 - \log_2(x - 2) = -1 + \log_2 x \rightarrow 3 = \log_2(x^2 - 2x)$$

$$8 = x^2 - 2x \rightarrow (x - 4)(x + 2) \rightarrow x = 4 \rightarrow y = 1$$

$$C = \frac{\log 32}{\log_{x^2} x} \cdot \frac{\log_{x^2} 16}{\log 32} = y = \frac{\log_{x^2} 16}{\frac{1}{2}}$$

$$y = 2 \log_{x^2} 16 \rightarrow 2 \log_{x^2} 2^4 \rightarrow y = 8 \log_{x^2} 2 \rightarrow \frac{y}{8} = \log_{x^2} 2 \rightarrow 5 \log_{x^2} 2 \rightarrow \frac{5}{8} y$$

$$1 \bullet 2 \bullet \frac{5}{8} y = \frac{5}{4} y$$

$$8. \begin{vmatrix} 1 & 2 & -1 & 1 \\ 3 & 4 & 2 & 0 \\ -2 & -3 & 5 & 0 \\ 2 & 1 & -1 & 0 \end{vmatrix} = - \begin{vmatrix} 3 & 4 & 2 \\ -2 & -3 & 5 \\ 2 & 1 & -1 \end{vmatrix} = -34$$

$$\begin{pmatrix} 1 & 1 & -1 \\ -3 & 2 & -1 \\ 3 & -3 & 2 \end{pmatrix} \text{ sum equals } 1.$$

$$-34 + 1 = -33$$

$$9. 2x - y = 6 \rightarrow 2x = y + 6 \rightarrow x = \frac{y+6}{2} \quad 4\left(\frac{x+6}{2}\right)^2 - 8\left(\frac{x+6}{2}\right) + 1 = x^2 + 12x + 36 - 4x - 24 + 1$$

$$x^2 + 8x + 13 \rightarrow \frac{-b}{a} = -8$$

$$(x^2 - 9)(x^4 - 3x^2 - 4) = (x - 3)(x + 3)(x^2 - 4)(x^2 + 1) \rightarrow 4$$

$$(x^2 + x - 2 - (x^2 - x - 6))(x^2 + x - 2 + x^2 - x - 6) (2x + 4)(2x^2 - 8) = 4(x + 2)(x - 2)(x + 2)$$

The absolute value of the difference between the largest and smallest is 4.  $-8 + 4 + 4 = 0$

10. Square both sides and you get:  $x - y + 2\sqrt{xy}i = 9 + 4\sqrt{5}i$  real component must be equal so  
 $x - y = 9$

$$\sqrt{5^2 + 2^2} \cdot \sqrt{2^2 + 5^2} = 29$$

$$i^{2010} = i^2 = -1 \rightarrow -2010$$

$$5 - x - 4i - yi = 2 \rightarrow 5 - x = 2 \rightarrow x = 3 \rightarrow y = -4 \rightarrow -1$$

$$9 + 29 - 2010 - 1 = -1973$$

11. Probably best to go to  $r \operatorname{cis} \theta$  form to answer this.  $(\sqrt{3}^2 + 1^2) = 4 \rightarrow \sqrt{4} = 2 \rightarrow 2^9 = 512 = r$

$$\tan \theta = \frac{y}{x} = \frac{1}{-\sqrt{3}} \rightarrow \arctan \frac{1}{-\sqrt{3}} \rightarrow \theta = 150; 9 \cdot 150 = 1350 \rightarrow 1350 - 1080 = 270 \rightarrow (0, -i)$$

$$512(0 - i) = 0 - 512i$$

$$20 \left( \cos \frac{11\pi}{6} + \sin \frac{11\pi}{6} \right) = 20 \left( \frac{\sqrt{3}}{2} - \frac{1}{2}i \right) = 10\sqrt{3} - 10i$$

$$0 - 512 + 10\sqrt{3} - 10 = -522 + 10\sqrt{3}$$

12.  $y^2 - 6y + 9 = -8x - 25 + 9 \rightarrow (y - 3)^2 = -8(x + 2)$ : The area of the triangle formed will be equal to  $\frac{1}{2}p(4p) = 2p^2$  where "p" is the distance from the vertex to the focus. Since  $4p = 8 \rightarrow p = 2 \rightarrow$  area equals 8.

$$9(x^2 - 2x + 1) + 25(y^2 - 6y + 9) = -9 + 9 + 225 \frac{(x-1)^2}{25} + \frac{(y-3)^2}{9} = 1 \rightarrow a = 5 \rightarrow b = 3 \rightarrow c = 4$$

$$\text{The area of the rectangle will be: } \frac{2b^2}{a} \cdot 2c = \frac{4b^2c}{a} = \frac{144}{5}$$

$$\frac{144}{5} = \frac{18}{5}$$

13. Treat 450-499 as one case and 500-699 as another:  $1 \cdot 4 \cdot 6 + 2 \cdot 6 \cdot 6 = 96$

$$3 \cdot 2 \cdot 1 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 = 720$$

$${}_{10}C_3 - {}_6C_3 = 120 - 20 = 100$$

$$96 + 720 + 100 = 916$$

$$14. \cos \theta = \frac{1+2+0}{\sqrt{6} \cdot \sqrt{2}} = \frac{\sqrt{3}}{2} \rightarrow \theta = \frac{\pi}{6}$$

Draw a triangle in QII since the inverse of Cotangent being negative is in that quadrant. The

triangle is a 1, 4 and  $\sqrt{17}$  triangle.  $\csc \theta = \frac{\sqrt{17}}{1} = \sqrt{17}$

Since “r” is the distance from the pole  $r = 12$ . The angle is 270 but since the directions asked for negative angle we must go with  $-90$  degrees.

$$\frac{\pi}{6} \cdot \sqrt{17} \cdot 12 \cdot -90 = -180\pi\sqrt{17}$$