

The following were changed at the resolution center at the convention: 26 A or B

- 1) $\int_9^{16} \frac{1}{\sqrt{x-4}} dx \Rightarrow \int_5^{12} u^{-1/2} du \Rightarrow 4\sqrt{3} - 2\sqrt{5}$ A
- 2) $y_{ave} = \frac{1}{3-1} \int_1^3 (2+x-x^2) dx = \frac{1}{2} (6+9/2+1/3-2-1/2-1) = 11/3$ A
- 3) $\int_0^5 (|2-x|) dx = \int_0^2 (2-x) dx - \int_2^5 (2-x) dx = [(4-2) - (10-25/2 - (4-2))] = 13/2$ D
- 4) $\int_0^4 \sqrt{x^2+1} dx \approx .5[1+2\sqrt{2}+2\sqrt{5}+2\sqrt{10}+\sqrt{17}]$ where $\Delta x = (4-0)/2(4) = .5$ C
- 5) $\int_1^9 e^{\sqrt{x}} dx = 2 \int_1^3 ue^u du = 2[3e^3 - e^3 - (e - e)] = 4e^3$ D
- 6) $V = 2\pi \int_0^e xe^x dx = 2\pi [xe^x - e^x] \Big|_0^e = 2\pi [e^{e+1} - e^e + 1]$ E
- 7) $\int_1^{e^\pi} (e^\pi/x - \ln x + e^{-\pi}) dx = e^\pi - e^{-\pi} = 2[(e^\pi - e^{-\pi})/2] = 2\sinh \pi$ B
- 8) $y' = \cos(\pi x^3)$ & $y'_{x=2} = \cos(8\pi) = 1$; so at $(2, 0)$, tangent line equation is $x - y = 2$ C
- 9) $\int_{\pi/2}^{3\pi/4} \sin^2 2t dt = \frac{1}{4} \int_{\pi}^{3\pi/2} (1 - \cos 2u) du = \frac{1}{4} (u - \frac{1}{2} \sin 2u) \Big|_{\pi}^{3\pi/2} = \frac{\pi}{8}$ D
- 10) $\int \frac{\log_{10}(x^4 10^x)}{x} dx = \frac{4}{\ln 10} \int \frac{\ln x}{x} dx + \int 1 dx = \frac{2}{\ln 10} (\ln x)^2 + x + C$ B
- 11) Improper integral, $\int_0^2 \frac{1}{(2x-1)^{2/3}} dx = \int_0^{1/2} \frac{1}{(2x-1)^{2/3}} dx + \int_{1/2}^2 \frac{1}{(2x-1)^{2/3}} dx = 3/2 + 3\sqrt[3]{3}/2$ D
- 12) $\frac{du}{dt} = \frac{t+3t^2}{u^2} \Rightarrow u^3/3 = t^2/2 + t^3 + C \Rightarrow C = 216 \Rightarrow u = (3t^2/2 + 3t^3 + 216)^{1/3}$ C
- 13) So the x^{12} term of $[x^3/2 - 2]^8 = \binom{8}{4} \left(\frac{x^3}{2}\right)^4 (-2)^4 = 70t^{12}$ and the coefficient of x^{13} is $70/13$ C
- 14) $\int \cos x \csc x dx = \int \cot x dx = \ln |\sin x| + C$ B
- 15) So A = $\frac{1}{2} \int_{-\pi/3}^{\pi/3} [(1+2\cos\theta)^2 - 2^2] d\theta = \int_0^{\pi/3} (4\cos\theta + 4\cos^2\theta - 3) d\theta = \frac{15\sqrt{3} - 2\pi}{6}$ D

$$16) \int_1^3 \frac{x+1}{x^2+2x+3} dx \Rightarrow \frac{1}{2} \int_6^{18} \ln |u| du = \frac{1}{2} (\ln 18 - \ln 6) = \ln \sqrt{3} \quad \text{B}$$

$$17) A(t) = t + \cos(2t) \Rightarrow v(t) = t^2/2 + (\sin(2t))/2 + C_1 \Rightarrow C_1 = 0; x(t) = t^3/6 - (\cos(2t))/4 + C_2 \text{ \& } C_2 = 1/4; \text{ so } x(\pi) = \pi^3/6 \quad \text{C}$$

$$18) \int_0^1 \int_0^{\pi/2} (e^y + \sin x) dx dy = \int_0^1 [\pi e^y / 2 - \cos(\pi/2) - (0 - 1)] dy = \pi e/2 + 1 - \pi/2 \quad \text{A}$$

$$19) A = \int_{-2}^1 [(3-x^2) - (x+1)] dx = 2 - 1/3 - 1/2 - (-6 + 8/3 - 2) = 9/2 \quad \text{C}$$

$$20) \text{ Given } g(x) = \int_1^{2x^2} (t-4) dt, g'(x) = (2x^2 - 4)(4x) = 0 \Rightarrow x = \pm \sqrt{2/3} \text{ and } g''(x) > 0 \text{ on } (-\infty, -\sqrt{2/3}) \cup (\sqrt{2/3}, \infty) \quad \text{B}$$

$$21) \text{ Using l'Hopital's Rule, } \lim_{x \rightarrow 1} \frac{\int_1^x 2(t \ln t - t + e^{t-1} + \pi) dt}{x^2 - 1} \Rightarrow \lim_{x \rightarrow 1} \frac{x \ln x - x + e^{x-1} + \pi x}{x} = \pi \quad \text{B}$$

$$22) \int \frac{x}{(2x+d)^2} dx = \frac{1}{2} \int \frac{1}{(2x+d)} dx - \frac{1}{2} \int \frac{1}{(2x+d)^2} dx = \frac{1}{4} \ln |2x+d| + \frac{d}{4(2x+d)} + C \quad \text{A}$$

$$23) \text{ TD} = \int_{-2}^3 |4t^3| dt = - \int_{-2}^0 4t^3 dt + \int_0^3 4t^3 dt = 16 + 81 = 97 \quad \text{D}$$

$$24) \text{ Since } f^{-1}(x) = e^x/\pi, \text{ then } \int f^{-1}(x) dx = \int \frac{e^x}{\pi} dx = e^x/\pi + C \quad \text{A}$$

$$25) A = \int_0^2 (4-x^2) dx = 16/3; \text{ so } A/2 = 8/3 \Rightarrow 8/3 = \int_c^4 \sqrt{y} dy \Rightarrow c = \sqrt[3]{16} \quad \text{C}$$

$$26) V = 2 \int_0^1 [(1-x^4) - (1-x^2)]^2 dx = 2 \int_0^1 (x^2 - x^4)^2 dx \quad \text{B}$$

$$27) \int \sin^3 x \cos^{-4} x dx = \int \sin x \cos^{-4} x dx - \int \sin x \cos^{-2} x dx = (\sec^3 x)/3 - \sec x + C \quad \text{D}$$

$$28) \text{ SA} = 2\pi \int_0^1 t^3 \sqrt{1+(3t^2)^2} dt = \frac{\pi}{18} \int_1^{10} t^3 \sqrt{u} du = \frac{\pi(10^{3/2} - 1)}{27} \quad \text{E}$$

$$29) \int_{-100}^{100} (v + \sin v + v \cos v + \sin^3 v)^5 dv = 0 \text{ (odd integrand with limits of } -a \text{ to } a \Rightarrow 0) \quad \text{A}$$

$$30) \int_0^{1/2} \frac{1}{1-x^2} dx = \tanh^{-1} x \Big|_0^{1/2} = \frac{1}{2} \left[\ln \left| \frac{1+x}{1-x} \right| \right]_0^{1/2} = \ln \sqrt{3} \quad C$$

