

**#0 Mu School Bowl**  
**MAΘ National Convention 2011**

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$$A = \lim_{x \rightarrow \infty} (\tan^{-1} x)$$

$$B = \lim_{x \rightarrow 2} \frac{x^2 + 8x - 20}{x^3 - 8}$$

$$C = \lim_{x \rightarrow 0^+} x^x$$

$$D = \lim_{x \rightarrow \pi} \tan x$$

Find the value of  $A + B + C + D$ .

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For the displacement function  $f(t) = 2t^2 - 3t - 2$ , let:

$A$  = the average velocity over the interval  $[1,2]$

$B$  = the instantaneous velocity at  $t = 1$

$C$  = the average velocity over the interval  $[2,3]$

$D$  = the instantaneous velocity at  $t = 2$

Find the value of  $\frac{A-B}{C-D}$ .

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Find the value of  $\frac{A-B}{C-D}$ .

**#2 Mu School Bowl**  
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$$A = \lim_{x \rightarrow -1} \frac{x^3 + x + 2}{2x^4 + 3x + 1}$$

$$B = f''(-3), \text{ where } f(x) = \frac{x-2}{x+1}$$

$$C = \text{the maximum value of } f(x) = -7x^{3/2} + 21x - 18$$

$$D = -1 + \text{the number of points of inflection of } f(x) = x^2 - 2x + 2x \ln x$$

Find the value of  $ABCD$ .

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Find the value of  $ABCD$ .

**#3 Mu School Bowl**  
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What is the minimum value of  $2x + y$ , given that  $xy = n$  and  $x$  and  $y$  are both positive?

$A =$  the solution when  $n = 50$

$B =$  the solution when  $n = 128$

$C =$  the solution when  $n = 162$

$D =$  the solution when  $n = 288$

Find the value of  $\frac{(A^2 + \sqrt{C})D}{B}$ .

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$D =$  the solution when  $n = 288$

Find the value of  $\frac{(A^2 + \sqrt{C})D}{B}$ .

**#4 Mu School Bowl**  
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For the function  $f(x) = x^3 - x^2 - x + 1$ :

$A$  = the sum of the  $x$ -intercepts of  $f$

$B$  = the sum of the  $x$ -coordinates of the relative extrema of  $f$

$C$  = the sum of the  $x$ -coordinates of the inflection points of  $f$

$D$  = the sum of the  $y$ -coordinates of all of the above points

Find the value of  $(4A + 3B + 3C)\sqrt{D}$ .

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Find the value of  $(4A + 3B + 3C)\sqrt{D}$ .

**#5 Mu School Bowl**  
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A diver jumps from a diving board 32 feet above water, and his position in feet at time  $t$  is determined by the function  $s(t) = -16t^2 + 24t + 32$ .

$A$  = the time  $t$  the diver hit the water

$B$  = the time  $t$  the diver was at the peak of his dive

$C$  = the diver's velocity on impact with the water

Find the value of  $\lfloor \lfloor A \rfloor B \rfloor \left( \frac{C}{8} \right)^2$ , where  $\lfloor x \rfloor$  represents the greatest integer  $n$  with  $n \leq x$ .

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**#6 Mu School Bowl**  
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For the function  $f(x) = \frac{\ln x}{x-1}$ , let  $L(x)$  be the linear approximation to the graph of  $f$  at  $x=e$ .

$A$  = the slope of  $y=L(x)$

$B$  = the  $x$ -intercept of  $y=L(x)$

$C$  = the  $y$ -intercept of  $y=L(x)$

$D=L(1)$

Find the value of  $\frac{A(B+e)}{CD}$ .

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$C$  = the  $y$ -intercept of  $y=L(x)$

$D=L(1)$

Find the value of  $\frac{A(B+e)}{CD}$ .

**#7 Mu School Bowl**  
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$$A = \int_1^3 \frac{x}{x^2 + 1} dx$$

$$B = \int_{-2}^1 (x^3 - 4x^2 + 2x - 3) dx$$

$$C = \int_{-2}^2 \frac{\tan^{-1} x}{1 + x^2} dx$$

$$D = \int_0^1 \left( \sum_{n=1}^{37} (n+1)x^n \right) dx$$

Find the value of  $\frac{Be^{2A}}{C+D}$ .

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Find the value of  $\frac{Be^{2A}}{C+D}$ .



**#8 Mu School Bowl**  
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Let  $f(x) = \int_2^x (t^4 + 3t^3 - 2t^2 + 17t - 14) dt$ . Find the value of  $f(2) + \sum_{n=1}^{\infty} f^{(n)}(2)$ .

**#8 Mu School Bowl**  
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Let  $f(x) = \int_2^x (t^4 + 3t^3 - 2t^2 + 17t - 14) dt$ . Find the value of  $f(2) + \sum_{n=1}^{\infty} f^{(n)}(2)$ .

**#9 Mu School Bowl**  
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Given the system of parametric equations  $\begin{cases} x = -t + \cos t \\ y = t^2 + \sin t \end{cases}$ , find the value of  $\frac{dy}{dx}\bigg|_{t=\frac{\pi}{2}} + \frac{d^2y}{dx^2}\bigg|_{t=\frac{\pi}{2}} + \frac{d^3y}{dx^3}\bigg|_{t=\frac{\pi}{2}}$ .

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**#10 Mu School Bowl**  
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Let  $f(x) = \frac{1}{4}x^2$  and  $g(x) = 2x - 3$ .

$A$  = the area bounded between  $f$  and  $g$

$B$  = the volume obtained by rotating the region bounded by  $f$  and  $g$  about the  $x$ -axis

$C$  = the volume obtained by rotating the region bounded by  $f$  and  $g$  about the  $y$ -axis

Find the value of  $\frac{AB}{C}$ .

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$C$  = the volume obtained by rotating the region bounded by  $f$  and  $g$  about the  $y$ -axis

Find the value of  $\frac{AB}{C}$ .

**#11 Mu School Bowl**  
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Consider the differential equation  $\frac{dy}{dx} = 2x - y$  with initial condition  $y(0) = 1$ . For each of the following, estimate the value of  $y(0.4)$ , using Euler's Method with given step size:

$A =$  solution with step size  $\Delta x = 0.4$

$B =$  solution with step size  $\Delta x = 0.2$

$C =$  solution with step size  $\Delta x = 0.1$

Find the value of  $A + B + C$ , written as a decimal.

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Find the value of  $A + B + C$ , written as a decimal.

**#12 Mu School Bowl**  
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List the letters of the series that converge.

$$A: \sum_{n=1}^{\infty} \frac{n}{n^3 + 1}$$

$$D: \sum_{n=1}^{\infty} \left(\frac{\pi}{4}\right)^n$$

$$B: \sum_{n=0}^{\infty} \frac{\cos(n\pi)}{n+1}$$

$$E: \sum_{n=1}^{\infty} (-1)^n e^{-n^2}$$

$$C: \sum_{n=1}^{\infty} \frac{(-3)^n}{(2n+1)!!}$$

$$F: \sum_{n=2}^{\infty} \frac{1}{\ln n}$$

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$$\text{Let } f(x) = \frac{\ln x}{x}.$$

$$A = f'(1)$$

$$B = \int_1^e f(t) dt$$

$$C = f'(e^2)$$

$$D = \int_1^{e^4} f(t) dt$$

Find the value of  $\frac{ABD}{C}$ .

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$$\text{Let } f(x) = \frac{\ln x}{x}.$$

$$A = f'(1)$$

$$B = \int_1^e f(t) dt$$

$$C = f'(e^2)$$

$$D = \int_1^{e^4} f(t) dt$$

Find the value of  $\frac{ABD}{C}$ .

**#14 Mu School Bowl**  
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$$\text{Let } f(x) = e^{1-x}.$$

$$A = f'(2011)$$

$$B = f''(2011)$$

$$C = f'''(2011)$$

$$D = f^{(4)}(2011)$$

$$\text{Find the value of } \frac{A}{B} + \frac{A}{C} + \frac{A}{D} + \frac{B}{A} + \frac{B}{C} + \frac{B}{D} + \frac{C}{A} + \frac{C}{B} + \frac{C}{D} + \frac{D}{A} + \frac{D}{B} + \frac{D}{C}.$$

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$$\text{Let } f(x) = e^{1-x}.$$

$$A = f'(2011)$$

$$B = f''(2011)$$

$$C = f'''(2011)$$

$$D = f^{(4)}(2011)$$

$$\text{Find the value of } \frac{A}{B} + \frac{A}{C} + \frac{A}{D} + \frac{B}{A} + \frac{B}{C} + \frac{B}{D} + \frac{C}{A} + \frac{C}{B} + \frac{C}{D} + \frac{D}{A} + \frac{D}{B} + \frac{D}{C}.$$

