

1.	C	$2x - 3y = 6$ $-3y = -2x + 6$ $y = \frac{2}{3}x + 6$ $\therefore \tan \theta = \frac{2}{3}, \cot \theta = \frac{3}{2}, \sin \theta = \frac{2}{\sqrt{13}}, \csc \theta = \frac{\sqrt{13}}{2}, \cos \theta = \frac{3}{\sqrt{13}}, \sec \theta = \frac{\sqrt{13}}{3}$
2.	A	
3.	A	$\begin{vmatrix} \sin \frac{3\pi}{2} & \sin 2\pi & \cos 4\pi \\ \left(\sin \frac{\pi}{3}\right)^2 & \sec 0 & \cot\left(\frac{3\pi}{4}\right) \\ \cos\left(\frac{9\pi}{2}\right) & \tan\left(-\frac{5\pi}{4}\right) & \left(\csc \frac{\pi}{4}\right)^4 \end{vmatrix} = \begin{vmatrix} -1 & 0 & 1 \\ \left(\frac{\sqrt{3}}{2}\right)^2 & 1 & -1 \\ 0 & -1 & (\sqrt{2})^4 \end{vmatrix} = \begin{vmatrix} -1 & 0 & 1 \\ \frac{3}{4} & 1 & -1 \\ 0 & -1 & 4 \end{vmatrix}$ $= -1 \begin{vmatrix} 1 & -1 \\ -1 & 4 \end{vmatrix} - 0 + 1 \begin{vmatrix} \frac{3}{4} & 1 \\ 0 & -1 \end{vmatrix} = -1(4 - 1) + 1\left(\frac{-3}{4} - 0\right) = -3 - \frac{3}{4} = \frac{-15}{4}$
4.	D	Using the Pythagorean theorem the missing side would be x. Therefore the answer is D.
5.	A	$A = \frac{1}{2}(4)(2)\sin 150^\circ = \frac{1}{2}(4)(2)\left(\frac{1}{2}\right) = 2$
6.	C	<p>A. Is neither even or odd</p> <p>B. Is even</p> <p>C. Is odd</p> <p>D. Is even</p>
7.	B	$\cos(75^\circ) = \sqrt{\frac{1 + \cos 150^\circ}{2}} = \sqrt{\frac{1 + \frac{-\sqrt{3}}{2}}{2}} = \frac{\sqrt{2 - \sqrt{3}}}{2}$
8.	B	$\cos^{-1}(\cos 225^\circ) = \cos^{-1}(-\sqrt{2}) = 135^\circ$
9.	D	<p><i>period</i> : <math>\frac{2\pi}{3\pi} = \frac{2}{3}</math></p> <p><i>frequeny</i> : <math>\frac{3}{2}</math></p> <p><i>amplitude</i> : 3</p> <p><math>\therefore \frac{2}{3} + \frac{3}{2} + 3 = \frac{31}{6}</math></p>

10.	B	$2012 \sin^2 x - 2012 = 0$ $2012(\sin x - 1)(\sin x + 1) = 0$ $\sin x = 1 \quad \sin x = -1$ $x = \frac{\pi}{2} \quad x = \frac{3\pi}{2}$
11.	C	$\frac{\csc \theta}{\sin^2 \theta + \sec \theta + \cos^2 \theta - 1}$ $\frac{\csc \theta}{\sin^2 \theta + \sec \theta - \sin^2 \theta}$ $\frac{1}{\sin \theta}$ $\frac{1}{\cos \theta}$ $\frac{\cos \theta}{\sin \theta}$ $\cot \theta$
12.	A	$\sin\left(\frac{\pi}{4} + x\right) + \sin\left(\frac{\pi}{4} - x\right)$ $\sin \frac{\pi}{4} \cos x + \cos \frac{\pi}{4} \sin x + \sin \frac{\pi}{4} \cos x - \cos \frac{\pi}{4} \sin x$ $2 \sin \frac{\pi}{4} \cos x$ $2 \left(\frac{\sqrt{2}}{2}\right) \cos x$ $\sqrt{2} \cos x$
13.	B	$2 \cos x \csc x - 4 \cos x - \csc x = -2 \text{ when } x \in [0, 2\pi)$ $2 \cos x \csc x - 4 \cos x - \csc x + 2 = 0$ $2 \cos x(\csc x - 2) - (\csc x - 2) = 0$ $(\csc x - 2)(2 \cos x - 1) = 0$ $\csc x = 2 \quad \cos x = \frac{1}{2}$ $x = \frac{\pi}{6}, \frac{5\pi}{6} \quad x = \frac{\pi}{3}, \frac{5\pi}{3}$
14.	C	

15.	B	$\cot 2\phi = \frac{0-0}{1}$ $\cot 2\phi = 0$ $2\phi = \frac{\pi}{2}$ $\phi = \frac{\pi}{4}$ $x' = x \cos \frac{\pi}{4} + y \sin \frac{\pi}{4}$ $x' = \frac{\sqrt{2}}{2}x + \frac{\sqrt{2}}{2}y$
16.	C	$d = \sqrt{5^2 + 2^2 - 2(2)(5)\cos(315^\circ - 45^\circ)}$ $d = \sqrt{25 + 4 - 20\cos(270^\circ)}$ $d = \sqrt{29 - 0}$ $d = \sqrt{29}$
17.	B	$2 + \sin x = 3 - \sin x$ $2\sin x = 1$ $\sin x = \frac{1}{2}$ $x = \frac{\pi}{6}, \frac{5\pi}{6}$
18.	D	
19.	A	
20.	B	$\cos^2 x - \sin^2 x$ $\left(\frac{-4}{7}\right)^2 - \left(\frac{-\sqrt{33}}{7}\right)^2$ $\frac{16}{49} - \frac{33}{49}$ $-\frac{17}{49}$
21.	D	I, II, and III

22.	C	$\cos x - \cos 2x = 2 \cos x$ $\cos x - (2 \cos^2 x - 1) = 2 \cos x$ $\cos x - 2 \cos^2 x + 1 = 2 \cos x$ $0 = 2 \cos^2 x + \cos x - 1$ $0 = (2 \cos x - 1)(\cos x + 1)$ $\cos x = \frac{1}{2} \quad \cos x = -1$ $x = \frac{\pi}{3}, \frac{5\pi}{3} \quad x = \pi$ $\therefore \frac{\pi}{3}, \pi$
23.	D	$\left( 6e^{i\left(\frac{4\pi}{3}\right)} \right)^2$ $(-3 - 3i\sqrt{3})^2$ $9 + 18i\sqrt{3} + 27i^2$ $9 + 18i\sqrt{3} + 27(-1)$ $9 + 18i\sqrt{3} - 27$ $-18 + 18i\sqrt{3}$
24.	C	$2(8)=16$
25.	A	$\langle 5, 2 \rangle$ and $\langle -1, 4 \rangle$ $\cos \theta = \frac{-5 + 8}{\sqrt{29} \cdot \sqrt{17}}$ $\cos \theta = \frac{3}{\sqrt{493}}$ $\cos \theta = \frac{3\sqrt{493}}{493}$
26.	C	Inner loop limaçon
27.	D	$\langle -12, 12 \rangle$ $12\sqrt{2} \operatorname{cis} \frac{3\pi}{4}$
28.	D	$\left( 81e^{i\frac{\pi}{3}} \right)^{1/4}$ $\text{roots: } 3 \operatorname{cis} \frac{\pi}{12}, 3 \operatorname{cis} \frac{7\pi}{12}, 3 \operatorname{cis} \frac{13\pi}{12}$

29.	B	$x = \frac{\pi}{2}$ shifted $\frac{\pi}{3}$ to the right results in $x = \frac{5\pi}{6} + \pi n$
30.	C	$\lim_{x \rightarrow 0} \frac{\sin 2x}{\sin x}$ $\lim_{x \rightarrow 0} \frac{2 \sin x \cos x}{\sin x}$ $\lim_{x \rightarrow 0} 2 \cos x$ $2 \cos(0)$ $2(1)$ $2$